

TIME ALLOWED: 3 HOURS

{ OPEN BOOKS }

**ATTEMPT ALL PROBLEMS:**

**PROBLEM #1:**

The stress function :

$$\Phi = (S/4c^2) [ c^2xy - cxy^2 - xy^3 + cly^2 + ly^3 ]$$

is proposed as giving the solution for a cantilever ( $y = \pm c$ ,  $0 < x < \ell$ ) loaded by uniform shear along the lower edge, the upper edge and the end  $x = \ell$  being free from load. In what respects is this solution imperfect? Compare the expressions for the stresses with those obtainable from elementary tension and bending formulas.

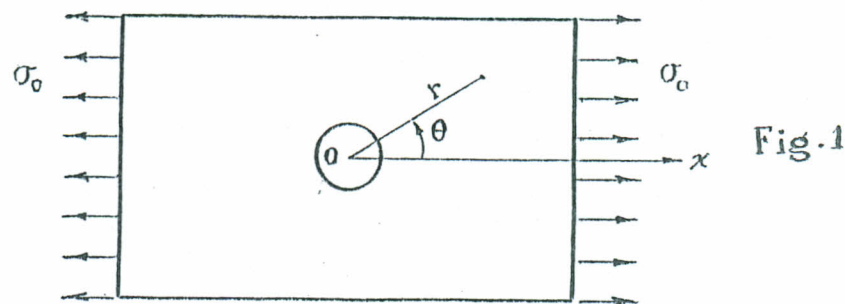
**PROBLEM #2:**

The stress function:

$$\Phi = (\sigma_0/2) [ (\frac{1}{2}r^2 - a^2 \ln r) + (-\frac{1}{2}r^2 - \frac{1}{2}(a^4/2r^2) + a^2) \cos 2\theta ]$$

is proposed as giving the solution for a large thin plate containing a small circular hole of radius (a) and subjected to simple tension as shown in Fig.1.

- Determine the stress field ( $\sigma_{rr}$ ,  $\sigma_{\theta\theta}$ ,  $\tau_{r\theta}$ ) in the plate,
- Calculate the stress concentration factor at the hole.



**PROBLEM #3:**

Consider a material which undergoes linear strain hardening. Its true stress- true strain curve in tension is given by:

$$\sigma = Y + 1.35 Y \epsilon$$

The stress - strain curve does not depend on strain rate.

- At what value of true strain will necking start?
- Suppose a stepped tensile bar (Fig.2) is made from this material. The initial cross-sectional area of region 1 is 0.990 times the initial cross-sectional area of region 2. What is the strain in region 2 when the strain in region 1 reaches 0.200 ?

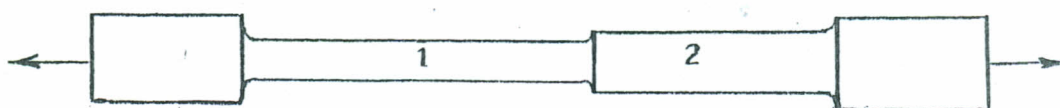


Fig.2

**PROBLEM #4:**

A steel sheet was deformed plastically. After unloading, it was found that the principal "engineering" strains in the plane of the sheet were  $e_1 = 0.172$  and  $e_2 = -0.0431$ . Assume that the ratio of stresses,  $\alpha = \sigma_2 / \sigma_1$ , was held constant during unloading and that there was no stress normal to the sheet surface. Also, assume the Von Mises criterion.

- (a) Find the ratio,  $\alpha = \sigma_2 / \sigma_1$ , that prevailed during loading.
- (b) Find the ratio,  $\bar{\sigma} / \sigma_1$ , that prevailed during loading.
- (c) Find the effective strain.
- (d) Assume that the tensile stress – strain curve for this steel can be approximated by  $\sigma = 650 \epsilon^{0.22}$  (MPa). Find the value of  $\sigma_1$  just before unloading.

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**PROBLEM #5:**

Write technical notes on each of the following:

- (a) Stress invariants.
  - (b) Bauschinger effect.
  - (c) Airy stress function.
  - (d) Slab method for solving plasticity problems.
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*Best Wishes!*

*Prof. Dr. M. Shabara*